

Trigonometry

$$(1) \cos(\theta) = \frac{adj}{hyp}, \sin(\theta) = \frac{opp}{hyp}, \tan(\theta) = \frac{opp}{adj}$$

$$(2) hyp^2 = adj^2 + opp^2$$

Quadratic Formula:

$$Ax^2 + Bx + C = 0 \Rightarrow x = \frac{-B \pm \sqrt{B^2 - 4AC}}{2A}$$

Displacement, Velocity, Acceleration:

$$(1) \Delta \vec{r} = \vec{r}_f - \vec{r}_0$$

$$(2) \vec{v}_{avg} = \frac{\Delta \vec{r}}{\Delta t}$$

$$(3) \vec{a}_{avg} = \frac{\Delta \vec{v}}{\Delta t}$$

Kinematic Equations for constant acceleration:

$$(1) x_f = x_0 + v_0 t + \frac{1}{2} a t^2$$

$$(2) v_f = v_0 + a t$$

$$(3) v_f^2 = v_0^2 + 2a(x_f - x_0)$$

$$(4) x_f - x_0 = \frac{1}{2}(v_f + v_0)t$$

Work & Energy:

$$(1) W_{net} = \frac{1}{2} m v_f^2 - \frac{1}{2} m v_0^2 = \Delta K.E.$$

$$(2) W = \vec{F} \cdot \vec{s} \text{ (Const. Force)}$$

$$(3) W = \int_a^b \vec{F} \cdot d\vec{s} \text{ (Varying Force)}$$

$$(4) \Delta K.E. + \Delta U - W_{nc} = 0 \text{ (No Ext. Forces)}$$

$$(5) U_{Grav} = mgy \quad U_{Spring} = \frac{1}{2} kx^2$$

$$(6) \Delta U_{ab} = -W_{ab} = -\int_a^b \vec{F} \cdot d\vec{s}$$

$$(7) \vec{F} = -\nabla U = -\frac{\partial U}{\partial x} \hat{i} - \frac{\partial U}{\partial y} \hat{j} - \frac{\partial U}{\partial z} \hat{k}$$

Vector Products

$$(1) \vec{A} \cdot \vec{B} = |\vec{A}| |\vec{B}| \cos \phi_{AB} = A_x B_x + A_y B_y + A_z B_z$$

$$(2) |\vec{A} \times \vec{B}| = |\vec{A}| |\vec{B}| \sin \phi_{AB}$$

$$(3) \vec{A} \times \vec{B} = \det \begin{vmatrix} \hat{i} & \hat{j} & \hat{k} \\ A_x & A_y & A_z \\ B_x & B_y & B_z \end{vmatrix}$$

$$(4) \vec{v}_{inst} = \frac{d\vec{r}}{dt}, \vec{\omega}_{inst} = \frac{d\theta}{dt}$$

$$(5) \vec{a}_{inst} = \frac{d\vec{v}}{dt}, \alpha_{inst} = \frac{d\omega}{dt}$$

$$(6) |\vec{a}_{circular}| = \frac{v^2}{r}$$

Newton's Laws:

$$(1) \vec{F}_{net} = 0 \Rightarrow \vec{a} = 0$$

$$(2) \vec{F}_{net} = m\vec{a}$$

$$\vec{F}_{AB} = -\vec{F}_{BA}$$

Force Laws:

$$(1) \vec{F}_{friction} : \begin{matrix} = \mu_k N \\ \leq \mu_s N \end{matrix}$$

$$(2) \vec{F}_{Spring} = -k\vec{x}$$

$$(3) \vec{F}_{Grav} = \begin{matrix} mg \text{ (Earth's Surface)} \\ \frac{Gm_1 m_2}{r^2} \text{ (Otherwise)} \end{matrix}$$

Impulse & Momentum:

$$(1) \vec{F}_{net} = \frac{d\vec{p}}{dt}$$

$$(2) \vec{J}_{net} = F_{AVG} \Delta t = \int_0^t \vec{F}_{net} dt = m\vec{v}_f - m\vec{v}_i = \Delta\vec{p}$$

$$(3) \frac{d\vec{p}_{Total}}{dt} = 0 \text{ (No Ext. Forces)}$$

Center of Mass:

$$(1) \vec{F}_{net\ EXT} = M_{Total} \vec{a}_{CM}$$

$$(2) \vec{r}_{CM} = \frac{m_1 \vec{r}_1 + m_2 \vec{r}_2 + \dots}{m_1 + m_2 + \dots} = \frac{1}{M_{Total}} \int \vec{r} dm$$

$$(3) \rho = \frac{M}{V} = \frac{dm}{dV}$$

Moment of Inertia:

$$(1) I_z = \int r^2 dm$$

$$(2) I_{Parallel} = I_{CM} + Md^2$$

Kinematic Equations for constant acceleration:

$$(1) \theta_f = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2$$

$$(2) \omega_f = \omega_0 + \alpha t$$

$$(3) \omega_f^2 = \omega_0^2 + 2\alpha(\theta_f - \theta_0)$$

$$(4) \theta_f - \theta_0 = \frac{1}{2}(\omega_f + \omega_0)t$$

$$(5) s = r\theta, (\theta \text{ in radians})$$

$$(6) \vec{v}_T = \vec{\omega} \times \vec{r}$$

$$(7) \vec{a}_T = \vec{\alpha} \times \vec{r}$$

$$(8) a_R = \frac{v^2}{r}$$

Rotational Work & Energy:

$$(1) W_{net} = \int \tau_{net} d\theta = \frac{1}{2} I \omega_f^2 - \frac{1}{2} I \omega_0^2 = \Delta K.E._{Rotational}$$

Rotational Dynamics:

$$(1) \vec{\tau} = \vec{r} \times \vec{F}, |\vec{\tau}| = |\vec{r}| |\vec{F}| \sin \theta_{rF}$$

$$(2) \vec{\tau}_{net} = 0 \Rightarrow \vec{\alpha} = 0$$

$$(3) \vec{\tau}_{net} = I \vec{\alpha}$$

$$(4) \vec{\tau}_{AB} = -\vec{\tau}_{BA}$$

$$(5) \vec{L}_{Totf} = \sum I_f \vec{\omega}_f = \vec{L}_{Tot0} = \sum I_0 \vec{\omega}_0 \text{ (No Ext. Torques)}$$

Pressure & Fluids:

$$(1) \rho = \frac{dM}{dV}$$

$$(2) P = \frac{dF_{\perp}}{dA}$$

$$(3) F_B = \rho_{Fluid} g V_{Object}$$

$$(4) P_1 + \rho g h_1 + \frac{1}{2} \rho v_1^2 = P_2 + \rho g h_2 + \frac{1}{2} \rho v_2^2$$

Oscillations & S.H.M

$$(1) x(t) = A \cos(\omega t + \phi)$$

$$(2) T = \frac{1}{f} = \frac{2\pi}{\omega}$$

$$(3) T_{mass-spring} = 2\pi \sqrt{\frac{m}{k}}$$

$$(4) T_{pendulum} = 2\pi \sqrt{\frac{mgr_{cm}}{I}}$$

Temperature & Heat:

(1) $Q = mc\Delta T$

(2) $\Delta L = \alpha L_0 \Delta T$

(3) $PV = nkT$

(4) $\Delta E_{int} = W + Q$

